

U NIK 4700

L3 h13

Homogeneous Electromagnetic Wave

single frequency

$$\vec{E}(\vec{r}) = E_0 e^{j(\omega t - \vec{k} \cdot \vec{r})},$$

$$\vec{B}(\vec{r}) = B_0 e^{j(\omega t - \vec{k} \cdot \vec{r})},$$

[Source: Wikipedia]

where

- $\vec{r} = (x, y, z)$ and $\vec{k} = (k_x, k_y, k_z)$ so?
- j is the imaginary unit
- $\omega = 2\pi f$ is the angular frequency, [rad/s]
- f is the frequency [1/s]
- $e^{j\omega t} = \cos(\omega t) + j \sin(\omega t)$ is Euler's formula

with $c = \frac{c_0}{n} = \frac{1}{\sqrt{\mu\epsilon}}$ and $n = \sqrt{\frac{\mu\epsilon}{\mu_0\epsilon_0}}$

room for comments

- *What is the difference between a static and a dynamic field*

UNIK4700 - CWI Basics of Communication UNIK4700/UNIK9700 Intro

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Boundary Conditions

- What is happening on electrical walls, magnetic walls?

Scattering, reflection and diffraction (explain differences) are the three major components in wave propagation. Ideal reflection environments are characterised through $|r| = 1$, $\phi_r = 180^\circ$

Reflection

Diffraction

~~Scattering~~ rough surface, large particle corner

smooth in FM radio
rough in UMTS

Multipath

- scattering
- reflection
- diffraction

Received signal Amplitude vs. Phase

Phase of amplitude \rightarrow path length \rightarrow frequency

Received power

ideal reflection: $\Gamma_{\text{mirror}} = -1$ Phase 180°

UMTS

60 MHz \leq 4 x 15 MHz

6 x 10 MHz

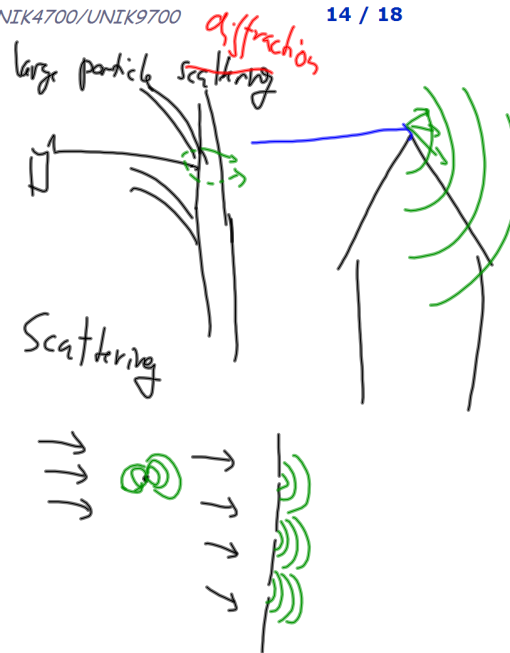
today = macro cells + micro cells

File in broadband area zone?

user from apartment by borderline in microworld

Basics of Communication
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Disturbance of EM wave

$\frac{d}{\lambda}$ ← diameter, length

$$\lambda = \frac{c}{f} = \frac{3 \times 10^8 \frac{m}{s}}{1 \times 10^9 \frac{1}{s}} = 0.3 \text{ m} = 30 \text{ cm}$$

$$\frac{\lambda}{20}, \frac{\lambda}{10} < \frac{d}{\lambda} < 2\lambda$$

Resonance: $d \sim \frac{\lambda}{2}, \lambda, 2\lambda$

f	λ	$\frac{\lambda}{2}$	$\frac{3\lambda}{2}$
100 MHz	3 m	1.5 m	4.5 m

"FM Radio"

$\frac{\lambda}{2} = 1.5 \text{ m}$

Interaction

$$\frac{\lambda}{90} \dots d \dots 2\lambda$$

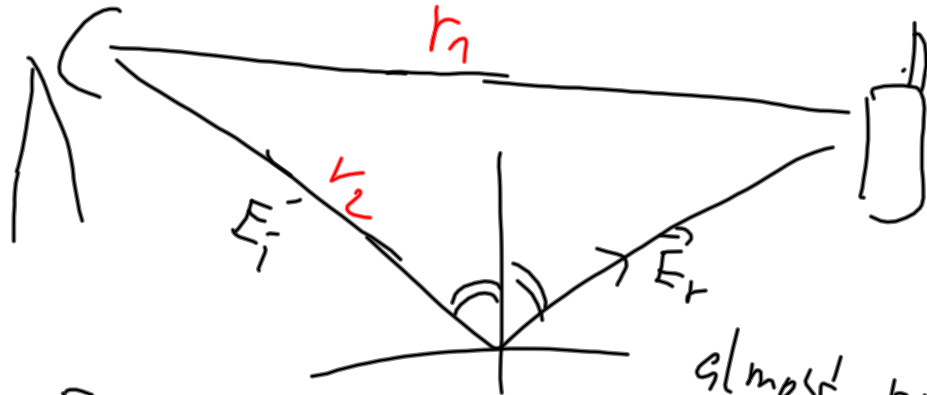
$$\lambda = \frac{30 \text{ cm}}{f [\text{GHz}]}$$

f	λ	$\frac{\lambda}{2}$	d _{range}	Interaction
100 MHz	3 m	1.5 m	30 cm ...	no full attenuation house, mountain
65M 900 ~ 16GHz	30 cm	15 cm	3 ... 60 cm	thick tree trunks, houses
1800 ~ 26GHz	15	7.5 cm	1.5 ... 30 cm	tree
UMTS 2100 ~ 2 kHz				
Wifi 2400 ~ 2.5 GHz	~12	6 cm	1.2 ... 24 cm	office wall
5100 ... 5600	6	3 cm	(6 mm) ... 12 cm	door, vegetation
LTE 2600				
(700)				Ultra Wifi Digital Divided Cognitive radio In TV

$$P_{dB} = 10 \log \frac{P}{1W}$$

$$P_{dBm} = 10 \log \frac{P}{1mW}$$

Perfect reflection



$$E_{tot} = E_d e^{-jk r_1} + E_r e^{-jk r_2}$$

\uparrow
 $r \cdot E_i$

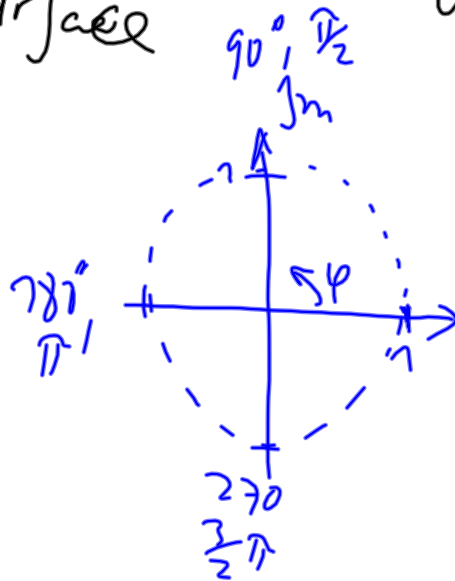
$$j = \sqrt{-1}$$

perfect w/ E_i

$$r = \frac{E_r}{E_i} = -1$$

perfectly flat

almost perfectly flat
sq surface



$$E_{tot} = E_0 (1 - e^{-jk \Delta r})$$

$\Delta r = 0, \lambda, 2\lambda, \dots$

$$E_{tot} = 0$$

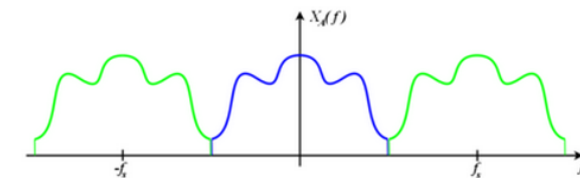
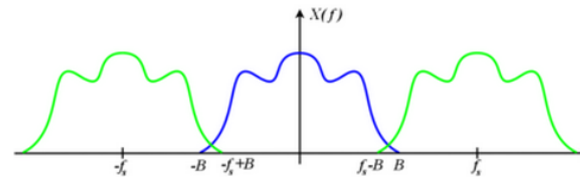
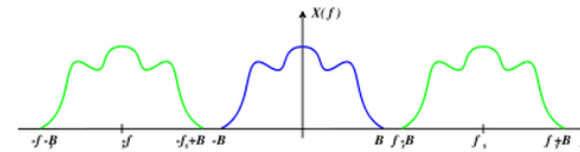
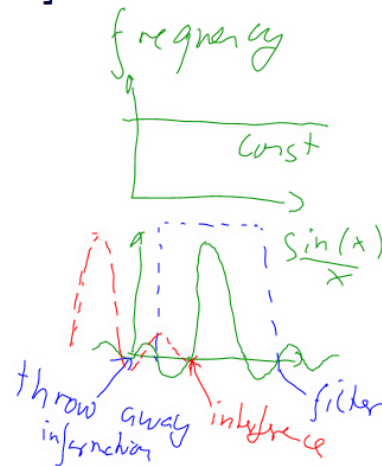
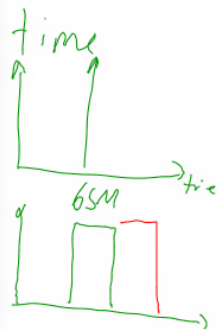
$$e^{+j\varphi} = \cos \varphi + j \sin \varphi$$

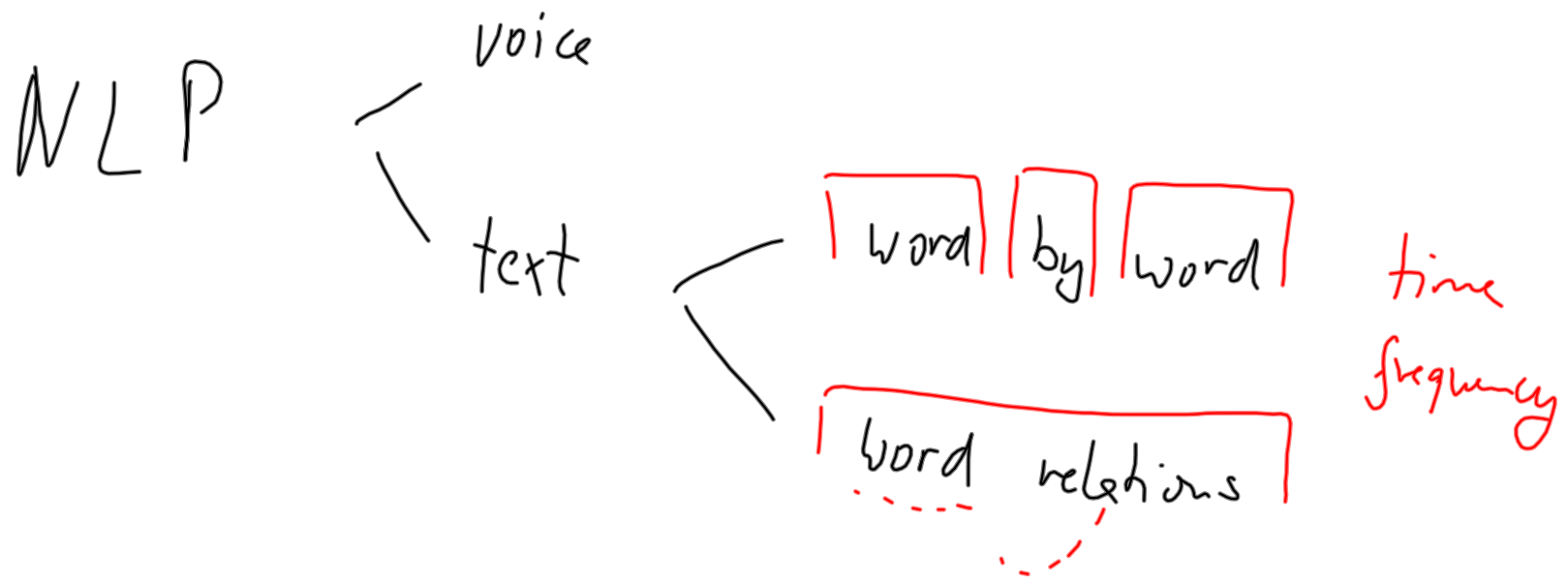
rad $\hat{=}$ 180°
deg

Nyquist Theorem

- Shannon: If a function $f(t)$ contains no frequencies higher than W [cycles/s], it is completely determined by giving its ordinates at series of points spaced $\frac{1}{2W}$ seconds apart
- band-limitation versus time-limitation
- → Fourier transform

[source: Shannon, 1948]





Signal/Noise Ratio

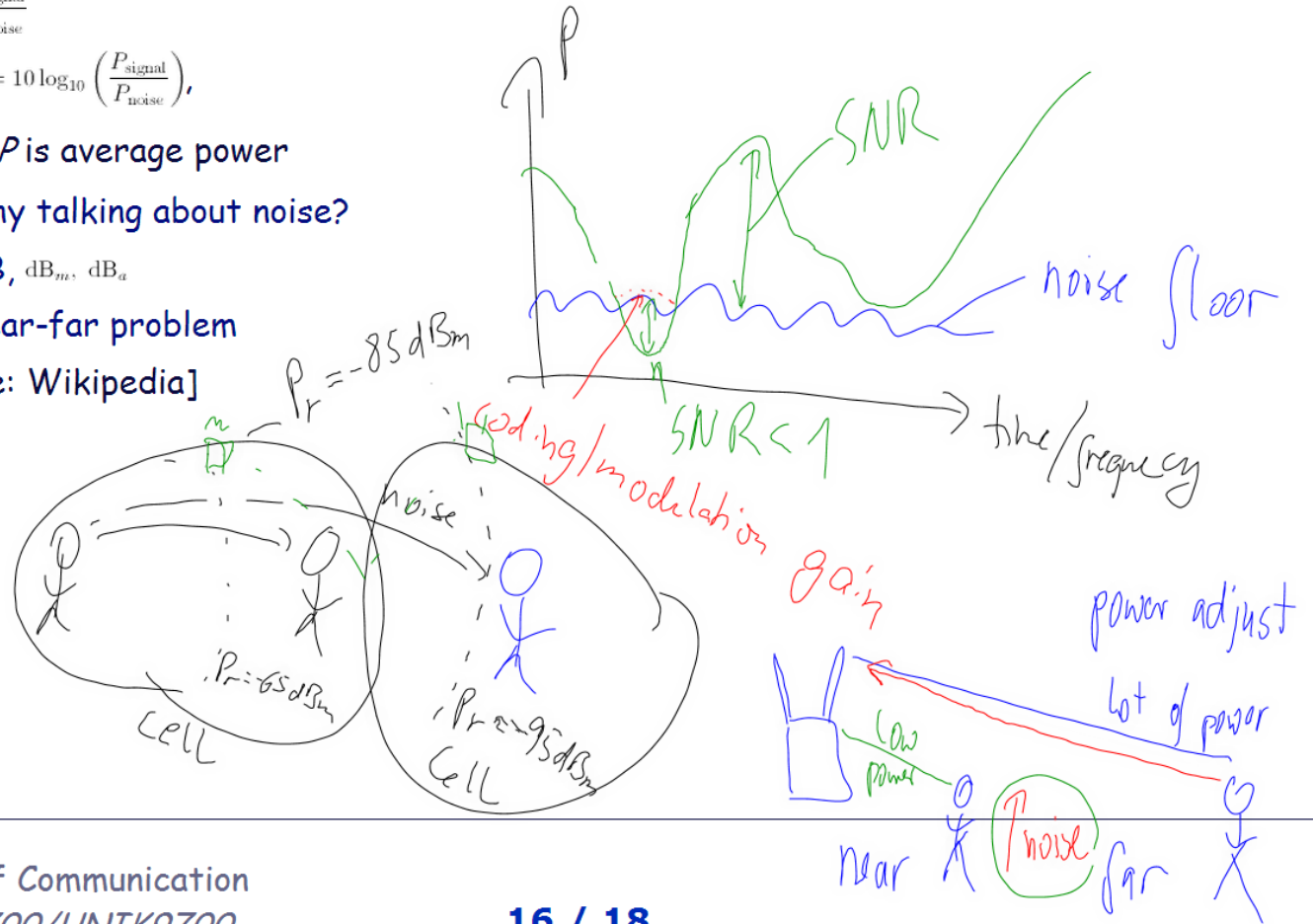
$$SNR = \frac{P_{\text{signal}}}{P_{\text{noise}}}$$

$$SNR(\text{dB}) = 10 \log_{10} \left(\frac{P_{\text{signal}}}{P_{\text{noise}}} \right),$$

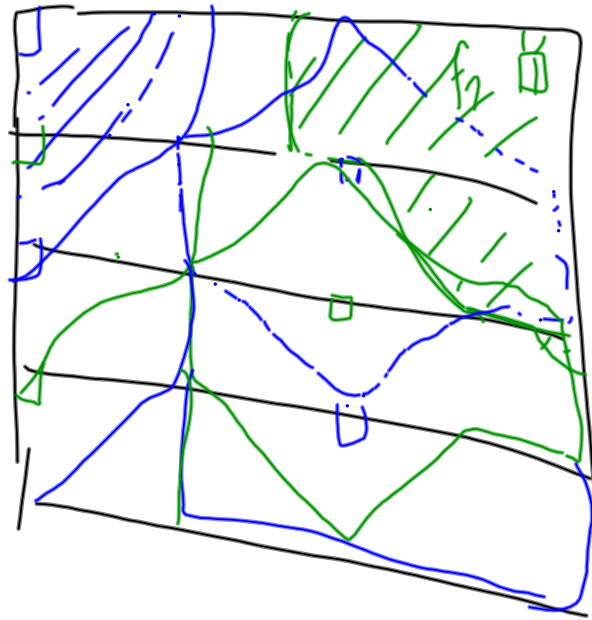
where P is average power

- why talking about noise?
- dB, dB_m, dB_a
- near-far problem

[source: Wikipedia]



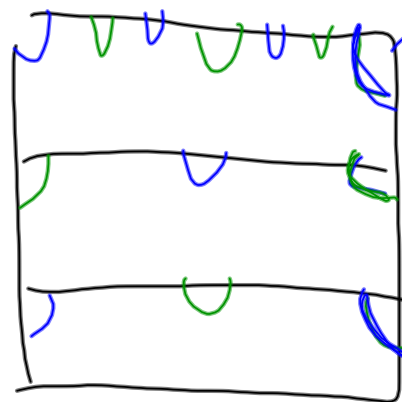
office building



range $\sim \frac{1}{2}$ building length

2 freq

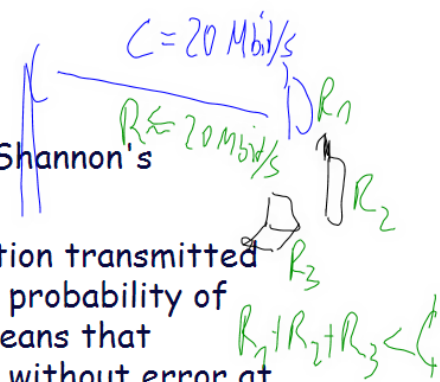
Lots of users
"Capacity" 3 freq



lower power of each
2 freq

frequency re farming

Shannon Theorem



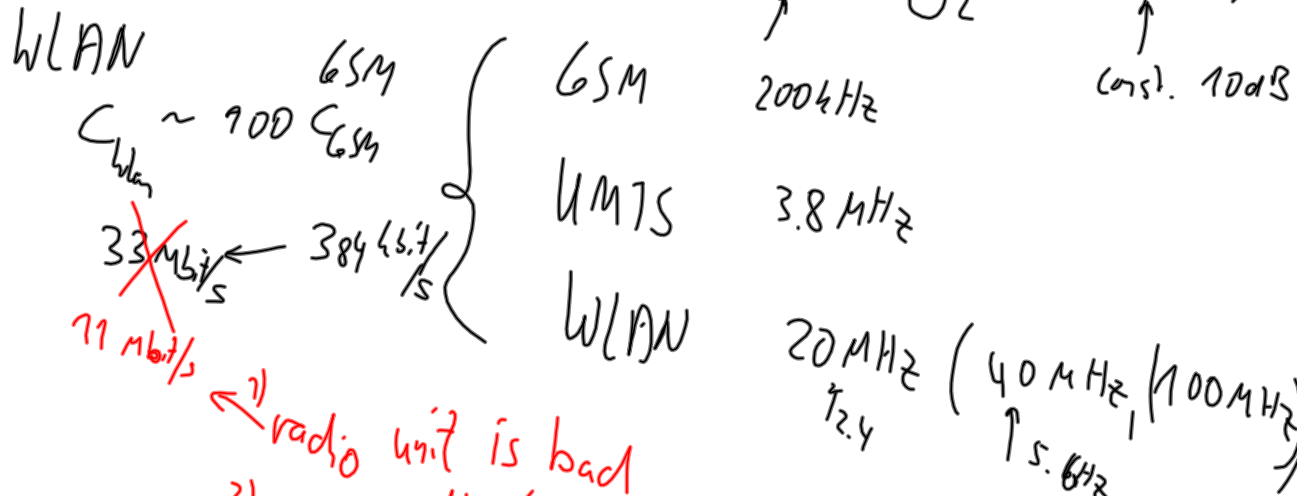
- The fundamental theorem of information theory, or just Shannon's theorem, was first presented by Claude Shannon in 1948.
- Given a noisy channel with channel capacity C and information transmitted at a rate R , then if $R < C$ there exist codes that allow the probability of error at the receiver to be made arbitrarily small. This means that theoretically, it is possible to transmit information nearly without error at any rate below a limiting rate, C .
- See File: [LarsLundheim-Telektronikk2002.pdf](#): The channel capacity of a band-limited information transmission channel with additive white, Gaussian noise. This capacity is given by an expression often known as "Shannon's formula": $C = W \log_2(1 + P/N)$ [bits/s]
W bandwidth
SNR
with W as system bandwidth, and $P/N = \frac{P}{N_0W}$ in case of interference free environment, otherwise $N_0W + N_{\text{interference}}$, where $N_0 = k_B T_K$ with k_B as Boltzmann constant and T_K as temperature in Kelvin.

Exercises:

- If the SNR is 20 dB, and the bandwidth available is 4 kHz, what is the capacity of the channel?
- If it is required to transmit at 50 kbit/s and a bandwidth of 1 MHz is

Shannon

$$C = \underbrace{B}_{\substack{\uparrow \\ \text{2004 Hz}}} \cdot \log_2 (1 + \underbrace{\text{SNR}}_{\substack{\uparrow \\ \text{const. 10 dB}}})$$

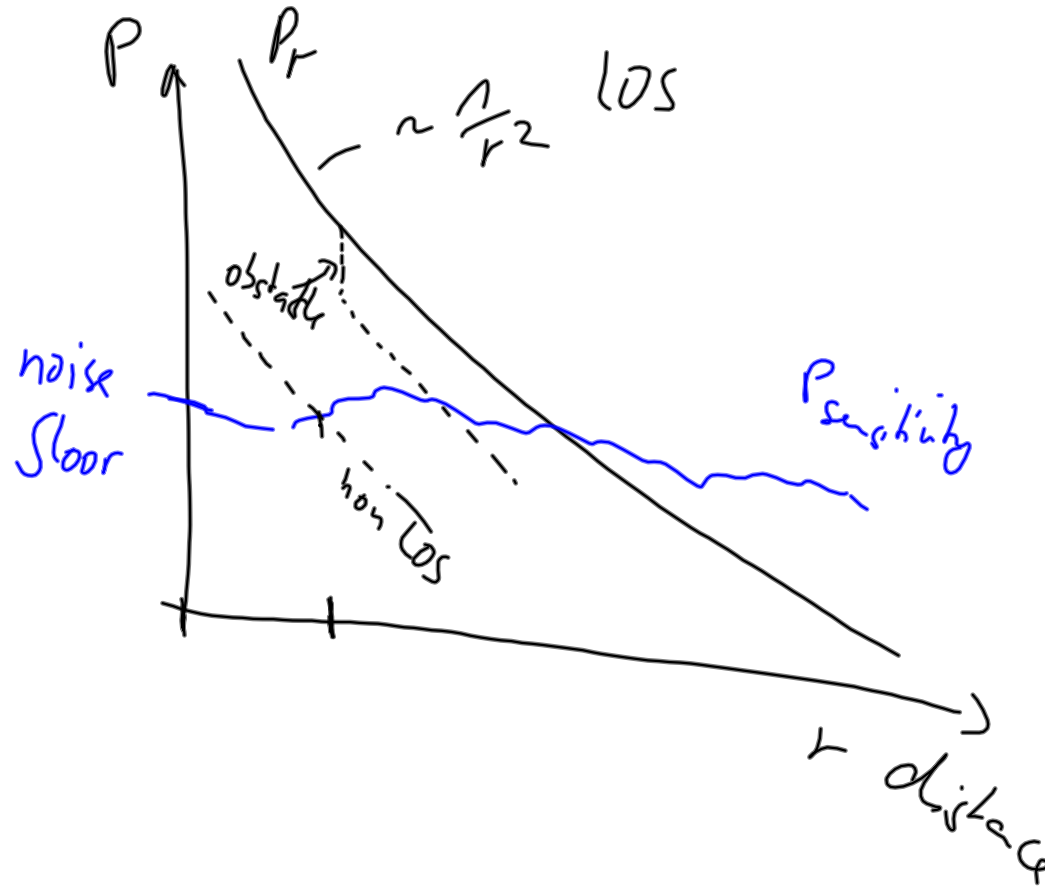


1) radio unit is bad
 2) GSM coding/modulation gain in GSM is higher

UMTS ~ 20 C
 $8 \text{ Mbit/s} \leftarrow 384 \text{ kbit/s}$
 2008: UMTS < 2 Mbit/s
 typical 7 Mbit/s
 2011: HSPA 8 Mbit/s
 2012: HSPA+ 12 Mbit/s \leftarrow higher coding/modulation gain

Radio propagation

$$P \sim \frac{1}{r^2}$$



$$C = W \log_2(1 + SNR)$$

40dB

0dB